

# NAG Fortran Library Routine Document

## G13FAF

**Note:** before using this routine, please read the Users' Note for your implementation to check the interpretation of ***bold italicised*** terms and other implementation-dependent details.

### 1 Purpose

G13FAF estimates the parameters of either a standard univariate regression GARCH process, or a univariate regression-type I AGARCH( $p, q$ ) process (see Engle and Ng (1993)).

### 2 Specification

```

SUBROUTINE G13FAF(DIST, YT, X, LDX, NUM, IP, IQ, NREG, MN, ISYM, NPAR,
1          THETA, SE, SC, COVAR, LDC, HP, ET, HT, LGF, COPTS,
2          MAXIT, TOL, WORK, LWORK, IFAIL)
  INTEGER      LDX, NUM, IP, IQ, NREG, MN, ISYM, NPAR, LDC, MAXIT,
1          LWORK, IFAIL
  real       YT(NUM), X(LDX,*), THETA(NPAR), SE(NPAR), SC(NPAR),
1          COVAR(LDC,NPAR), HP, ET(NUM), HT(NUM), LGF, TOL,
2          WORK(LWORK)
  LOGICAL      COPTS(2)
  CHARACTER*1  DIST

```

### 3 Description

A univariate regression-type I AGARCH( $p, q$ ) process, with  $q$  coefficients  $\alpha_i$ , for  $i = 1, \dots, q$ ,  $p$  coefficients  $\beta_i$ , for  $i = 1, \dots, p$ , and  $k$  linear regression coefficients  $b_i$ , for  $i = 1, \dots, k$ , can be represented by:

$$y_t = b_o + x_t^T b + \epsilon_t \quad (1)$$

$$h_t = \alpha_0 + \sum_{i=1}^q \alpha_i (\epsilon_{t-i} + \gamma)^2 + \sum_{i=1}^p \beta_i h_{t-i}, \quad t = 1, \dots, T \quad (2)$$

where  $\epsilon_t | \psi_{t-1} = N(0, h_t)$  or  $\epsilon_t | \psi_{t-1} = S_t(df, h_t)$ . Here  $S_t$  is a standardised Student's  $t$ -distribution with  $df$  degrees of freedom and variance  $h_t$ ,  $T$  is the number of terms in the sequence,  $y_t$  denotes the endogenous variables,  $x_t$  the exogenous variables,  $b_o$  the regression mean,  $b$  the regression coefficients,  $\epsilon_t$  the residuals,  $h_t$  is the conditional variance,  $df$  the number of degrees of freedom of the Student's  $t$ -distribution, and  $\psi_t$  the set of all information up to time  $t$ .

G13FAF provides an estimate for  $\hat{\theta}$ , the parameter vector  $\theta = (b_o, b^T, \omega^T)$  where  $b^T = (b_1, \dots, b_k)$ ,  $\omega^T = (\alpha_0, \alpha_1, \dots, \alpha_q, \beta_1, \dots, \beta_p, \gamma)$  when DIST = 'N' and  $\omega^T = (\alpha_0, \alpha_1, \dots, \alpha_q, \beta_1, \dots, \beta_p, \gamma, df)$  when DIST = 'T'.

ISYM, MN and NREG can be used to simplify the GARCH( $p, q$ ) expression in (1) as follows:

#### No Regression and No Mean

$$y_t = \epsilon_t,$$

$$\text{ISYM} = 0,$$

$$\text{MN} = 0,$$

$$\text{NREG} = 0 \text{ and}$$

$$\theta \text{ is a } (p + q + 1) \text{ vector, when DIST = 'N' and a } (p + q + 2) \text{ vector, when DIST = 'T'.$$

**No Regression**

$$y_t = b_o + \epsilon_t,$$

$$\text{ISYM} = 0,$$

$$\text{MN} = 1,$$

$$\text{NREG} = 0 \text{ and}$$

$\theta$  is a  $(p + q + 2)$  vector when  $\text{DIST} = \text{'N'}$  and a  $(p + q + 3)$  vector, when  $\text{DIST} = \text{'T'}$ .

**Note:** if the  $y_t = \mu + \epsilon_t$ , where  $\mu$  is known (not to be estimated by G13FAF) then (1) can be written as  $y_t^\mu = \epsilon_t$ , where  $y_t^\mu = y_t - \mu$ . This corresponds to the case **No Regression and No Mean**, with  $y_t$  replaced by  $y_t - \mu$ .

**No Mean**

$$y_t = x_t^T b + \epsilon_t,$$

$$\text{ISYM} = 0,$$

$$\text{MN} = 0,$$

$$\text{NREG} = k \text{ and}$$

$\theta$  is a  $(p + q + k + 1)$  vector when  $\text{DIST} = \text{'N'}$  and a  $(p + q + k + 2)$  vector, when  $\text{DIST} = \text{'T'}$ .

**4 References**

Engle R (1982) Autoregressive conditional heteroskedasticity with estimates of the variance of United Kingdom inflation *Econometrica* **50** 987–1008

Bollerslev T (1986) Generalised autoregressive conditional heteroskedasticity *Journal of Econometrics* **31** 307–327

Engle R and Ng V (1993) Measuring and Testing the Impact of News on Volatility *Journal of Finance* **48** 1749–1777

Hamilton J (1994) *Time Series Analysis* Princeton University Press

**5 Parameters**

- 1: DIST – CHARACTER\*1 *Input*  
*On entry:* the type of distribution to use for  $e_t$ .  
 If DIST = 'N', a Normal distribution is used.  
 If DIST = 'T', a Student's  $t$ -distribution is used.  
*Constraint:* DIST = 'N' or 'T'.
- 2: YT(NUM) – *real* array *Input*  
*On entry:* the sequence of observations,  $y_t$ , for  $t = 1, \dots, T$ .
- 3: X(LDX,\*) – *real* array *Input*  
**Note:** the second dimension of the array X must be at least  $\max(1, \text{NREG} + \text{MN})$ .  
*On entry:* row  $t$  of X must contain the time dependent exogenous vector  $x_t$ , where  $x_t^T = (x_t^1, \dots, x_t^k)$ , for  $t = 1, \dots, T$ .
- 4: LDX – INTEGER *Input*  
*On entry:* the first dimension of the array X as declared in the (sub)program from which G13FAF is called.  
*Constraint:*  $\text{LDX} \geq \text{NUM}$ .

- 5: NUM – INTEGER Input  
*On entry:* the number of terms in the sequence,  $T$ .  
*Constraint:*  $\text{NUM} \geq \max(\text{IP}, \text{IQ})$ .
- 6: IP – INTEGER Input  
*On entry:* the number of coefficients,  $\beta_i$ , for  $i = 1, \dots, p$ .  
*Constraint:*  $\text{IP} \geq 0$  (see also NPAR).
- 7: IQ – INTEGER Input  
*On entry:* the number of coefficients,  $\alpha_i$ , for  $i = 1, \dots, q$ .  
*Constraint:*  $\text{IQ} \geq 1$  (see also NPAR).
- 8: NREG – INTEGER Input  
*On entry:* the number of regression coefficients,  $k$ .  
*Constraint:*  $\text{NREG} \geq 0$  (see also NPAR).
- 9: MN – INTEGER Input  
*On entry:* if  $\text{MN} = 1$ , the mean term  $b_0$  will be included in the model.  
*Constraint:*  $\text{MN} = 0$  or  $1$ .
- 10: ISYM – INTEGER Input  
*On entry:* if  $\text{ISYM} = 1$  then the asymmetry term  $\gamma$  will be included in the model.  
*Constraint:*  $\text{ISYM} = 0$  or  $1$ .
- 11: NPAR – INTEGER Input  
*On entry:* the number of parameters to be included in the model.  
 $\text{NPAR} = 1 + \text{IQ} + \text{IP} + \text{ISYM} + \text{MN} + \text{NREG}$  when  $\text{DIST} = \text{'N'}$ , and  
 $\text{NPAR} = 2 + \text{IQ} + \text{IP} + \text{ISYM} + \text{MN} + \text{NREG}$  when  $\text{DIST} = \text{'T'}$ .  
*Constraint:*  $\text{NPAR} < 20$ .
- 12: THETA(NPAR) – *real* array Input/Output  
*On entry:* the initial parameter estimates for the vector  $\theta$ . The first element must contain the coefficient  $\alpha_0$  and the next IQ elements must contain the coefficients  $\alpha_i$ , for  $i = 1, \dots, q$ . The next IP elements must contain the coefficients  $\beta_j$ , for  $j = 1, \dots, p$ . If  $\text{ISYM} = 1$ , then the next element must contain the asymmetry parameter  $\gamma$ . If  $\text{DIST} = \text{'T'}$ , then the next element must contain  $df$ , the number of degrees of freedom of the Student's  $t$ -distribution. If  $\text{MN} = 1$ , then the next element must contain the mean term  $b_0$ . If  $\text{COPTS}(2) = \text{.FALSE.}$ , then the remaining NREG elements are taken as initial estimates of the linear regression coefficients  $b_i$ , for  $i = 1, \dots, k$ .  
*On exit:* the estimated values  $\hat{\theta}$  for the vector  $\theta$ . The first element contains the coefficient  $\alpha_0$ , the next IQ elements contain the coefficients  $\alpha_i$ , for  $i = 1, \dots, q$ . The next IP elements are the coefficients  $\beta_j$ , for  $j = 1, \dots, p$ . If  $\text{ISYM} = 1$  then the next element contains the estimate for the asymmetry parameter  $\gamma$ . If  $\text{DIST} = \text{'T'}$  then the next element contains an estimate for  $df$ , the number of degrees of freedom of the Student's  $t$ -distribution. If  $\text{MN} = 1$  then the next element contains an estimate for the mean term  $b_0$ . The final NREG elements are the estimated linear regression coefficients  $b_i$ , for  $i = 1, \dots, k$ .
- 13: SE(NPAR) – *real* array Output  
*On exit:* the standard errors for  $\hat{\theta}$ . The first element contains the standard error for  $\alpha_0$ . The next IQ elements contain the standard errors for  $\alpha_i$ , for  $i = 1, \dots, q$ . The next IP elements are the standard errors for  $\beta_j$ , for  $j = 1, \dots, p$ . If  $\text{ISYM} = 1$ , then the next element contains the standard error for  $\gamma$ .

If  $DIST = 'T'$ , then the next element contains the standard error for  $df$ , the number of degrees of freedom of the Student's  $t$ -distribution. If  $MN = 1$ , then the next element contains the standard error for  $b_o$ . The final NREG elements are the standard errors for  $b_j$ , for  $j = 1, \dots, k$ .

- 14: SC(NPAR) – *real* array *Output*  
*On exit:* the scores for  $\hat{\theta}$ . The first element contains the score for  $\alpha_o$ . The next IQ elements contain the score for  $\alpha_i$ , for  $i = 1, \dots, q$ . The next IP elements are the scores for  $\beta_j$ , for  $j = 1, \dots, p$ . If  $ISYM = 1$ , then the next element contains the score for  $\gamma$ . If  $DIST = 'T'$  then the next element contains the score for  $df$ , the number of degrees of freedom of the Student's  $t$ -distribution. If  $MN = 1$ , then the next element contains the score for  $b_o$ . The final NREG elements are the scores for  $b_j$ , for  $j = 1, \dots, k$ .
- 15: COVAR(LDC,NPAR) – *real* array *Output*  
*On exit:* the covariance matrix of the parameter estimates  $\hat{\theta}$ , that is the inverse of the Fisher Information Matrix.
- 16: LDC – INTEGER *Input*  
*On entry:* the first dimension of the array COVAR as declared in the (sub)program from which G13FAF is called.  
*Constraint:*  $LDC \geq NPAR$ .
- 17: HP – *real* *Input/Output*  
*On entry:* if  $COPTS(2) = .FALSE.$ , then HP is the value to be used for the pre-observed conditional variance; otherwise HP is not referenced.  
*On exit:* if  $COPTS(2) = .TRUE.$ , then HP is the estimated value of the pre-observed of the conditional variance.
- 18: ET(NUM) – *real* array *Output*  
*On exit:* the estimated residuals,  $\epsilon_t$ , for  $t = 1, \dots, T$ .
- 19: HT(NUM) – *real* array *Output*  
*On exit:* the estimated conditional variances,  $h_t$ , for  $t = 1, \dots, T$ .
- 20: LGF – *real* *Output*  
*On exit:* the value of the log likelihood function at  $\hat{\theta}$ .
- 21: COPTS(2) – LOGICAL array *Input*  
*On entry:* the options to be used by G13FAF.  
 If  $COPTS(1) = .TRUE.$ , stationary conditions are enforced, otherwise they are not.  
 If  $COPTS(2) = .TRUE.$ , the routine provides initial parameter estimates of the regression terms, otherwise these are provided by the user.
- 22: MAXIT – INTEGER *Input*  
*On entry:* the maximum number of iterations to be used by the optimization routine when estimating the GARCH( $p, q$ ) parameters. If MAXIT is set to 0 then the standard errors, score vector and variance-covariance are calculated for the input value of  $\theta$  in THETA; however the value of  $\theta$  is not updated.  
*Constraint:*  $MAXIT \geq 0$ .

- 23: TOL – *real* *Input*  
*On entry:* the tolerance to be used by the optimization routine when estimating the GARCH( $p, q$ ) parameters.
- 24: WORK(LWORK) – *real* array *Workspace*  
 25: LWORK – INTEGER *Input*  
*On entry:* the dimension of the array WORK as declared in the (sub)program from which G13FAF is called.  
*Constraint:*  $LWORK \geq (NREG + 3) \times NUM + NPAR + 403$ .
- 26: IFAIL – INTEGER *Input/Output*  
*On entry:* IFAIL must be set to 0, -1 or 1. Users who are unfamiliar with this parameter should refer to Chapter P01 for details.  
*On exit:* IFAIL = 0 unless the routine detects an error (see Section 6).  
 For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, because for this routine the values of the output parameters may be useful even if IFAIL  $\neq$  0 on exit, the recommended value is -1. **When the value -1 or 1 is used it is essential to test the value of IFAIL on exit.**

## 6 Error Indicators and Warnings

If on entry IFAIL = 0 or -1, explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

IFAIL = 1

On entry, NREG < 0,  
 or MN > 1,  
 or MN < 0,  
 or ISYM > 1,  
 or ISYM < 0,  
 or IQ < 1,  
 or IP < 0,  
 or NPAR  $\geq$  20,  
 or NPAR has an invalid value,  
 or LDC < NPAR,  
 or LDX < NUM,  
 or DIST  $\neq$  'N',  
 or DIST  $\neq$  'T',  
 or MAXIT < 0,  
 or NUM < max(IP, IQ).

IFAIL = 2

On entry,  $LWORK < (NREG + 3) \times NUM + NPAR + 403$ .

IFAIL = 3

The matrix  $X$  is not full rank.

IFAIL = 4

The information matrix is not positive definite.

IFAIL = 5

The maximum number of iterations has been reached.

IFAIL = 6

The log-likelihood cannot be optimised any further.

IFAIL = 7

No feasible model parameters could be found.

## 7 Accuracy

Not applicable.

## 8 Further Comments

None.

## 9 Example

This example program uses G05HKF to generate 1500 data points, with known process parameters  $\theta$  for the following two time-series:

- (i) An ARCH(3) sequence with normally distributed residuals.
- (ii) A GARCH(1,2) sequence with Student's  $t$ -distributed residuals.

Here G05HKF is initially called, with the output discarded, to eliminate 'start-up effects' in these sequences. The process parameter estimates,  $\hat{\theta}$ , are then obtained using G13FAF, and compared with their true values,  $\theta$ . Finally a four step ahead volatility estimate is computed using G13FBF.

### 9.1 Program Text

**Note:** the listing of the example program presented below uses *bold italicised* terms to denote precision-dependent details. Please read the Users' Note for your implementation to check the interpretation of these terms. As explained in the Essential Introduction to this manual, the results produced may not be identical for all implementations.

```
*      G13FAF Example Program Text
*      Mark 20 Release. NAG Copyright 2001.
*      .. Parameters ..
INTEGER          NOUT
PARAMETER       (NOUT=6)
INTEGER         NPARMX, NUM
real           ZERO
PARAMETER       (NPARMX=10,NUM=1500,ZERO=0.0e0)
INTEGER         NUM1, NREGMX
PARAMETER       (NUM1=3000,NREGMX=10)
*      .. Local Scalars ..
real          DF, FAC1, GAMMA, HP, LGF, MEAN, TOL, XTERM
INTEGER         I, IFLAG, IGEN, IP, IQ, ISYM, K, LDX, LWK, MAXIT,
+              MN, NPAR, NPAR2, NREG, NT
LOGICAL         FCALL
CHARACTER       DIST
*      .. Local Arrays ..
real          BX(10), COVAR(NPARMX,NPARMX), CVAR(100),
+              ETM(NUM1), HT(NUM1+10), HTM(NUM1), PARAM(NPARMX),
+              RVEC(40), RWSAV(9), SC(NPARMX), SE(NPARMX),
+              THETA(NPARMX), WK(NUM1*3+NPARMX+NREGMX*NUM1+20*
+              20+1), X(NUM1,10), YT(NUM1+10)
INTEGER         ISEED(4)
LOGICAL         COPTS(2)
*      .. External Subroutines ..
EXTERNAL        G05CBF, G05HKF, G05KBF, G13FAF, G13FBF
*      .. Intrinsic Functions ..
INTRINSIC       real, SIN
```

```

*    .. Executable Statements ..
WRITE (NOUT,*) 'G13FAF Example Program Results'

ISEED(1) = 111
IGEN = 0

NREG = 0
LDX = NUM1
BX(1) = 1.5e0
BX(2) = 2.5e0
BX(3) = 3.0e0
MEAN = 3.0e0
DO 20 I = 1, NUM
    FAC1 = real(I)*0.01e0
    X(I,1) = 0.01e0 + 0.7e0*SIN(FAC1)
    X(I,2) = 0.5e0 + FAC1*0.1e0
    X(I,3) = 1.0e0
20 CONTINUE

ISYM = 1
MN = 1
GAMMA = -0.4e0
IP = 0
IQ = 3
PARAM(1) = 0.8e0
PARAM(2) = 0.6e0
PARAM(3) = 0.2e0
PARAM(4) = 0.1e0

NPAR = 1 + IQ + IP

LWK = NREG*NUM + 3*NUM + NPAR + ISYM + MN + NREG + 403

FCALL = .TRUE.
IFLAG = 0
DIST = 'N'

CALL G05KBF(IGEN,ISEED)

CALL G05HKF(DIST,NUM,IP,IQ,PARAM,GAMMA,DF,HT,YT,FCALL,RVEC,IGEN,
+          ISEED,RWSAV,IFLAG)

FCALL = .FALSE.
CALL G05HKF(DIST,NUM,IP,IQ,PARAM,GAMMA,DF,HT,YT,FCALL,RVEC,IGEN,
+          ISEED,RWSAV,IFLAG)

IFLAG = -1

DO 60 I = 1, NUM
    XTERM = ZERO
    DO 40 K = 1, NREG
        XTERM = XTERM + X(I,K)*BX(K)
40    CONTINUE
    IF (MN.EQ.1) THEN
        YT(I) = MEAN + XTERM + YT(I)
    ELSE
        YT(I) = XTERM + YT(I)
    END IF
60 CONTINUE

COPTS(1) = .TRUE.
COPTS(2) = .TRUE.

MAXIT = 200
TOL = 1.0e-5

DO 80 I = 1, NPAR
    THETA(I) = PARAM(I)*0.5e0
80 CONTINUE

IF (ISYM.EQ.1) THEN

```

```

      THETA(NPAR+ISYM) = GAMMA*0.5e0
    END IF

    IFLAG = 0
    NPAR2 = 1 + IQ + IP + ISYM + MN + NREG
    CALL G13FAF(DIST,YT,X,LDX,NUM,IP,IQ,NREG,MN,ISYM,NPAR2,THETA,SE,
+             SC,COVAR,NPARMX,HP,ETM,HTM,LGF,COPTS,MAXIT,TOL,WK,LWK,
+             IFLAG)

    WRITE (NOUT,*)
    WRITE (NOUT,*) 'Normal distribution'
    WRITE (NOUT,*)
    WRITE (NOUT,*) '          Parameter          Standard          Correct'
    WRITE (NOUT,*) '          estimates          errors          values'

    DO 100 I = 1, NPAR
      WRITE (NOUT,99999) THETA(I), SE(I), PARAM(I)
100 CONTINUE

    IF (ISYM.EQ.1) THEN
      WRITE (NOUT,99999) THETA(NPAR+1), SE(NPAR+1), GAMMA
    END IF

    IF (MN.EQ.1) THEN
      WRITE (NOUT,99999) THETA(NPAR+ISYM+1), SE(NPAR+ISYM+1), MEAN
    END IF

    DO 120 I = 1, NREG
      WRITE (NOUT,99999) THETA(NPAR+ISYM+MN+I), SE(NPAR+ISYM+MN+I),
+             BX(I)
120 CONTINUE

    NT = 4
    CALL G13FBF(NUM,NT,IP,IQ,THETA,GAMMA,CVAR,HTM,ETM,IFLAG)

    WRITE (NOUT,*)
    WRITE (NOUT,99998) 'Volatility forecast = ', CVAR(NT)
    WRITE (NOUT,*)

    DIST = 'T'
    NREG = 2
    MN = 1
    DF = 4.1e0
    IP = 1
    IQ = 2
    ISYM = 1
    GAMMA = -0.2e0

    NPAR = IQ + IP + 1
    LWK = NREG*NUM + 3*NUM + NPAR + ISYM + MN + NREG + 404

    PARAM(1) = 0.1e0
    PARAM(2) = 0.2e0
    PARAM(3) = 0.3e0
    PARAM(4) = 0.4e0
    PARAM(5) = 0.1e0

    FCALL = .TRUE.
    CALL G05CBF(111)
    IGEN = 0
    ISEED(1) = 111
    CALL G05KBF(IGEN,ISEED)

    CALL G05HKF(DIST,NUM,IP,IQ,PARAM,GAMMA,DF,HT,YT,FCALL,RVEC,IGEN,
+             ISEED,RWSAV,IFLAG)
    FCALL = .FALSE.
    CALL G05HKF(DIST,NUM,IP,IQ,PARAM,GAMMA,DF,HT,YT,FCALL,RVEC,IGEN,
+             ISEED,RWSAV,IFLAG)
    CALL G05HKF(DIST,NUM,IP,IQ,PARAM,GAMMA,DF,HT,YT,FCALL,RVEC,IGEN,
+             ISEED,RWSAV,IFLAG)

```



```

IFLAG = -1
DO 160 I = 1, NUM
  XTERM = ZERO
  DO 140 K = 1, NREG
    XTERM = XTERM + X(I,K)*BX(K)
140  CONTINUE
  IF (MN.EQ.1) THEN
    YT(I) = MEAN + XTERM + YT(I)
  ELSE
    YT(I) = XTERM + YT(I)
  END IF
160 CONTINUE

COPTS(1) = .TRUE.
COPTS(2) = .TRUE.

MAXIT = 200
TOL = 1.0e-5

DO 180 I = 1, NPAR
  THETA(I) = PARAM(I)*0.5e0
180 CONTINUE

THETA(NPAR+ISYM) = GAMMA*0.5e0
THETA(NPAR+ISYM+1) = DF*0.65e0

NPAR2 = 2 + IP + IQ + ISYM + MN + NREG
CALL G13FAF(DIST,YT,X,LDX,NUM,IP,IQ,NREG,MN,ISYM,NPAR2,THETA,SE,
+          SC,COVAR,NPARMX,HP,ETM,HTM,LGF,COPTS,MAXIT,TOL,WK,LWK,
+          IFLAG)

WRITE (NOUT,*)
WRITE (NOUT,*) 'Student t-distribution'
WRITE (NOUT,*)
WRITE (NOUT,*) '          Parameter          Standard          Correct'
WRITE (NOUT,*) '          estimates          errors          values'

DO 200 I = 1, NPAR
  WRITE (NOUT,99999) THETA(I), SE(I), PARAM(I)
200 CONTINUE

IF (ISYM.EQ.1) THEN
  WRITE (NOUT,99999) THETA(NPAR+ISYM), SE(NPAR+ISYM), GAMMA
END IF

WRITE (NOUT,99999) THETA(NPAR+ISYM+1), SE(NPAR+ISYM+1), DF

IF (MN.EQ.1) THEN
  WRITE (NOUT,99999) THETA(NPAR+ISYM+1+MN), SE(NPAR+ISYM+1+MN),
+  MEAN
END IF

DO 220 I = 1, NREG
  WRITE (NOUT,99999) THETA(NPAR+ISYM+1+MN+I),
+  SE(NPAR+ISYM+1+MN+I), BX(I)
220 CONTINUE

NT = 4
CALL G13FBF(NUM,NT,IP,IQ,THETA,GAMMA,CVAR,HTM,ETM,IFLAG)

WRITE (NOUT,*)
WRITE (NOUT,99998) 'Volatility forecast = ', CVAR(NT)
STOP
*
99999 FORMAT (1X,3F16.4)
99998 FORMAT (1X,A,F12.4)
END

```

## 9.2 Program Data

None.

## 9.3 Program Results

G13FAF Example Program Results

Normal distribution

Parameter estimates	Standard errors	Correct values
0.8031	0.0788	0.8000
0.6249	0.0570	0.6000
0.1803	0.0327	0.2000
0.0921	0.0237	0.1000
-0.5119	0.0682	-0.4000
2.9860	0.0324	3.0000

Volatility forecast = 2.8040

Student t-distribution

Parameter estimates	Standard errors	Correct values
0.0871	0.0244	0.1000
0.2174	0.0549	0.2000
0.2736	0.0849	0.3000
0.3588	0.0811	0.4000
-0.3240	0.0650	-0.2000
4.5173	0.5238	4.1000
3.0182	0.0431	3.0000
1.4727	0.0269	1.5000
2.4640	0.0319	2.5000

Volatility forecast = 0.4133

---